23.63. Model: Use ray tracing to locate the image. Assume the diverging lens is a thin lens. Solve: (a)



The figure shows the ray-tracing diagram using the steps of Tactics Box 23.3. After refraction, the three special rays do not converge. The rays, on the other hand, appear to meet at a point that is 8.5 cm on the same side of the lens as the object. So s' = -8.5 cm. The image is upright and has a height of 1.1 cm. (b) Using the thin-lens formula,

$$\frac{1}{s} + \frac{1}{s'} = \frac{1}{f} \implies \frac{1}{15 \text{ cm}} + \frac{1}{s'} = \frac{1}{-20 \text{ cm}} \implies \frac{1}{s'} = -\frac{7}{60 \text{ cm}} \implies s' = -\frac{60}{7} \text{ cm} = -8.6 \text{ cm}$$

The image height is obtained from

$$M = -\frac{s'}{s} = -\frac{(-60 / 7 \text{ cm})}{15 \text{ cm}} = +\frac{4}{7} = 0.57$$

Thus, the image is 0.57 times larger than the object, or h' = Mh = (0.57)(2.0 cm) = 1.14 cm. The image is upright because *M* is positive. These values agree, within measurement accuracy, with those obtained in part (a).